

Classical Mechanics, PHYB54

Problem Set 2

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Due: Monday, January 23th 2017, 4pm

Note: Assignments can be hand-written, but illegible answers will not be marked. Clearly indicate your final answers.

Problem 1.1

- Use the series expansions of e^z to prove Euler's identity, $e^{i\pi} + 1 = 0$.
- Use the series expansions of e^z to prove $e^{u+v} = e^u e^v$.
- Using the previous results, write $\cos(u + v) + i \sin(u + v)$ in terms of $\cos(v)$, $\cos(u)$, $\sin(v)$, and $\sin(u)$.

Problem 1.2

- The masses of the Earth and Moon are approximately $M_e = 6.0 \times 10^{24}$ kg and $M_m = 7.4 \times 10^{22}$ kg. The center to center distance is approximately 3.8×10^5 km. Where is the center of mass if we assume the center of the Earth is the origin of the coordinate system.
- The Earth's distribution of mass is not symmetrical. One way to approximate this effect is to add a third body. Assume that along the direction of the Moon, we add a third body halfway with a mass which is a tenth of a percent of Earth's mass. What is the new center of mass of this system? Additionally, express this change in center of mass as a percentage (i.e. $\frac{\text{Two body system}}{\text{Three body system}}$). How significant is this correction?

Problem 1.3

A particle moves under the influence of a central force directed toward a fixed origin \mathbf{O} . Explain why the particle's angular momentum about \mathbf{O} is constant. Give in detail the argument that the particle's orbit must lie in a single plane containing \mathbf{O} .