

ASTC02 - PROF. HANNO REIN

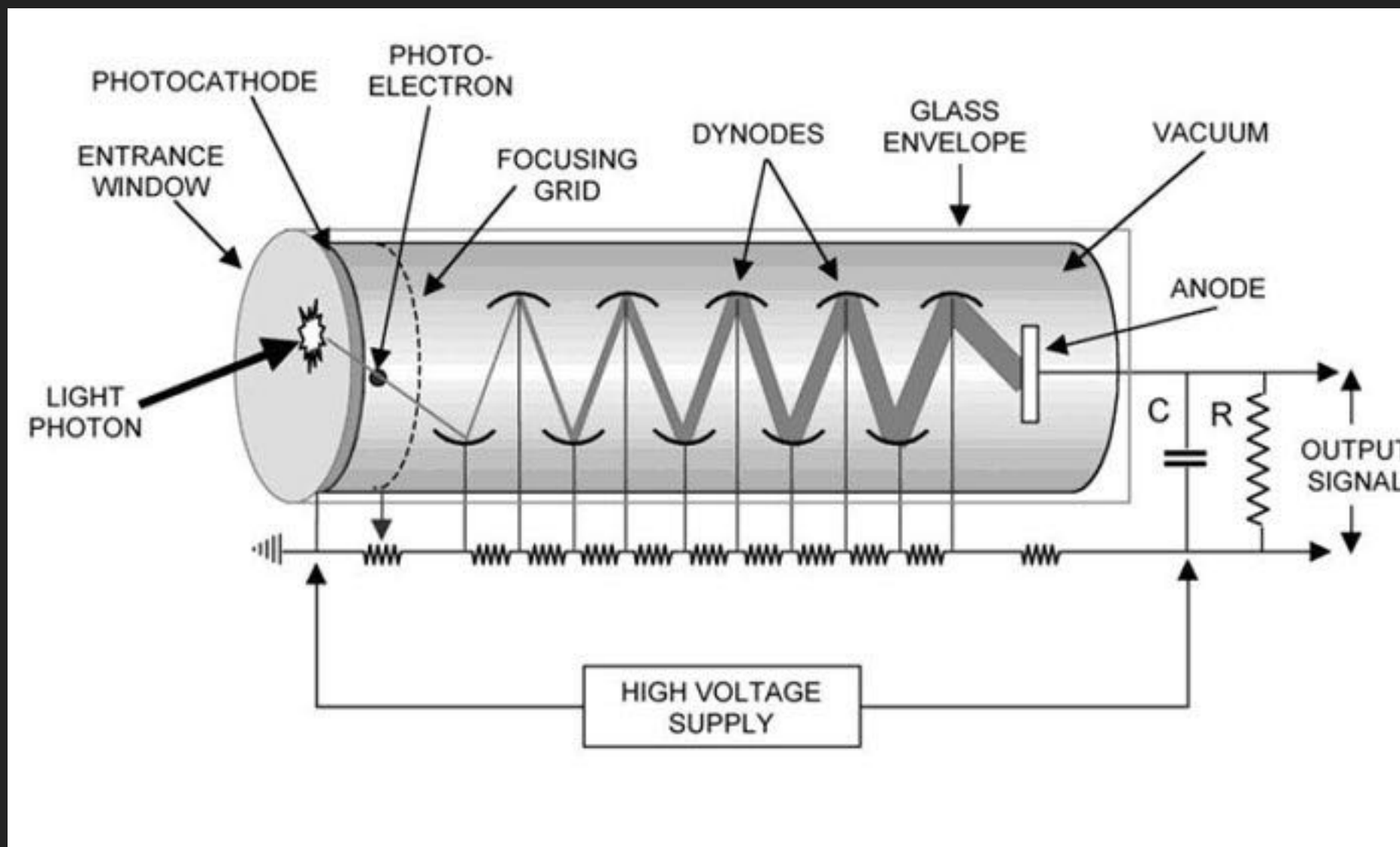
DETECTORS

BEFORE CCDS

Photographic plates for images

Photomultiplier tubes for photometry

PHOTOMULTIPLIER TUBES



PHOTOMULTIPLIER TUBES



DETECTOR SIZE / RESOLUTION

CCD (typical 2004)

- ▶ 2048 x 2048
- ▶ 15 μ m x 15 μ m
- ▶ 30mm x 30mm

CMOS (Canon 450D)

- ▶ 4272x2848
- ▶ 5.2 μ m x 5.2 μ m
- ▶ 22.2mm x 14.8 mm

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STATISTICS

STATISTICS

Precision with which a quantity is measured is important.

In this lecture: Frequentist approach

Better: Bayesian approach

DIFFERENT SOURCES OF NOISE

INSTRUMENTAL NOISE

Every instrument has background noise.

Need to measure the background noise, then subtract it.

Note that measuring the background noise has its own error associated with it!

INSTRUMENTAL NOISE

SYSTEMATIC

E.g. temperature changes

Unpredictable manner.

Can NOT be improved by more measurements.

STATISTICAL

E.g. random cosmic rays

Can be measured as accurately as desired.

But it may take a lot of time.

STATISTICAL FLUCTUATIONS

Inherent randomness of events

EXAMPLE: PHOTONS FROM A STAR (POISSON STATISTICS)

Well defined average number of photons that arrive on detector,
100 photons per second

If measured for finite time, will fluctuate from interval to interval

Assumption: all events are uncorrelated

Get distribution of counts $N(x)$: 105, 98, 87, 96, 103, 101, 97

EXAMPLE: PHOTONS FROM A STAR (POISSON STATISTICS)

Distribution of counts $N(x)$: 105, 98, 87, 96, 103, 101, 97

$$P_x = \frac{m^x e^{-m}}{x!}$$

Probability of detecting x events (integer) if the average is m .

If we collect 100 photons in a pixel on average, how likely is it that we collect exactly 100 in a single frame?

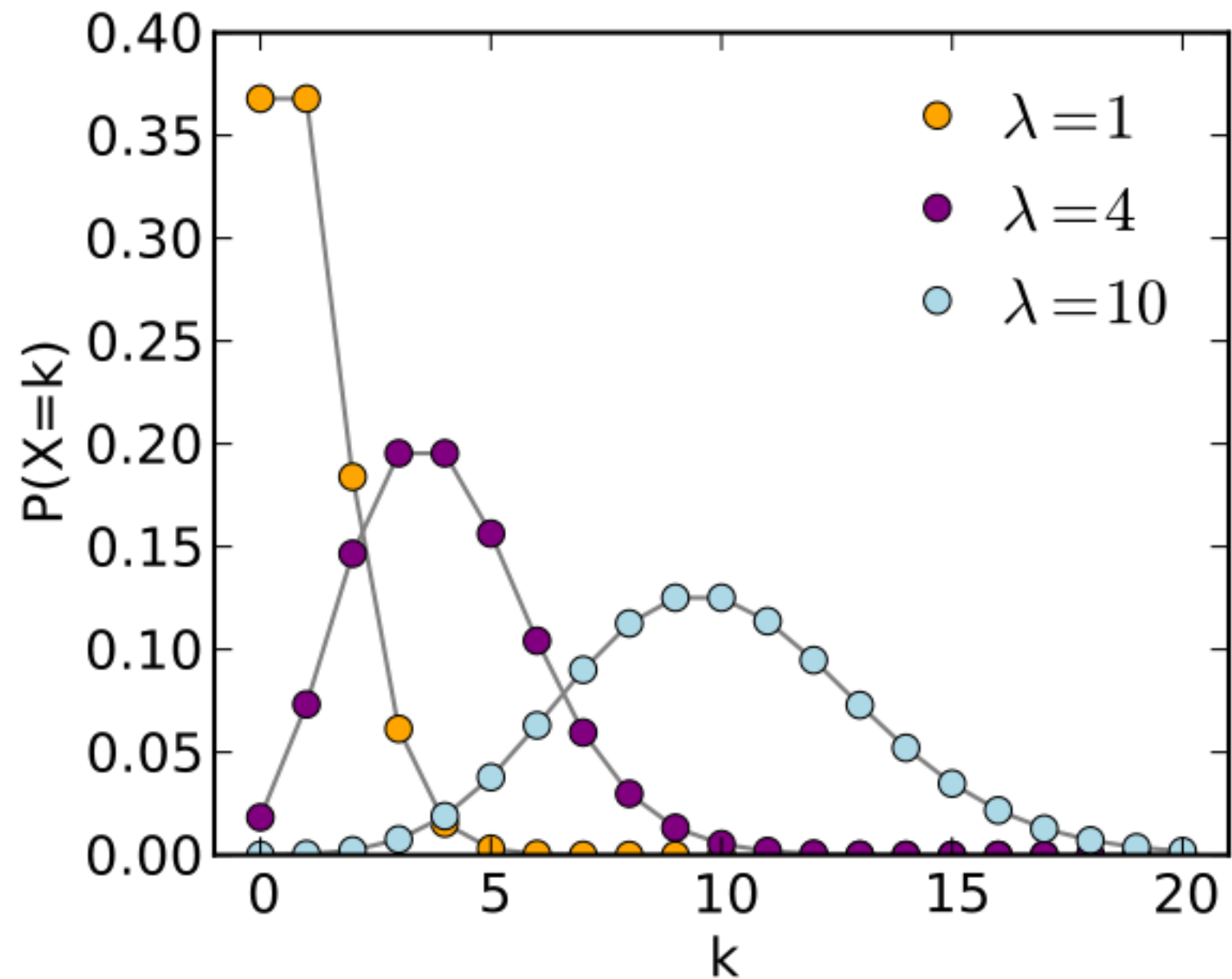
If we collect 6 photons in a pixel on average, how likely is it that we collect exactly 6 in a single frame?

EXAMPLE: PHOTONS FROM A STAR (POISSON STATISTICS)

$$P_x = \frac{m^x e^{-m}}{x!}$$

Note that:

$$\sum_{x=0}^{\infty} P_x = 1$$



NORMAL DISTRIBUTION

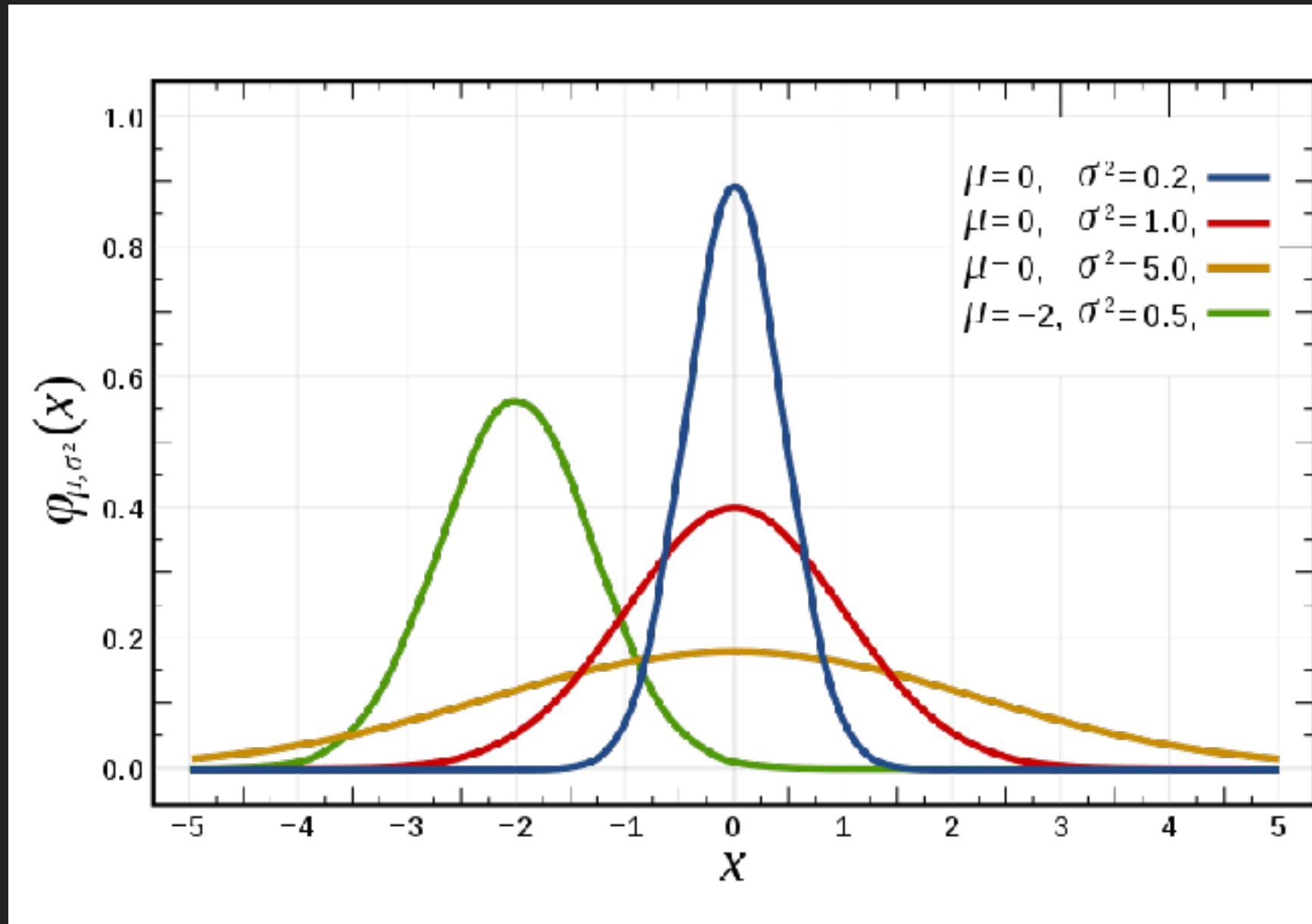
$$dP_x = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x-m)^2}{2\sigma^2}\right)$$

$$\int_{x=-\infty}^{x=+\infty} dP_x = 1$$

- Continuous → differential probability
- Two parameters, m and σ
- Symmetric
- Will give negative values!

NORMAL DISTRIBUTION

$$dP_x = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x - m)^2}{2\sigma^2}\right)$$

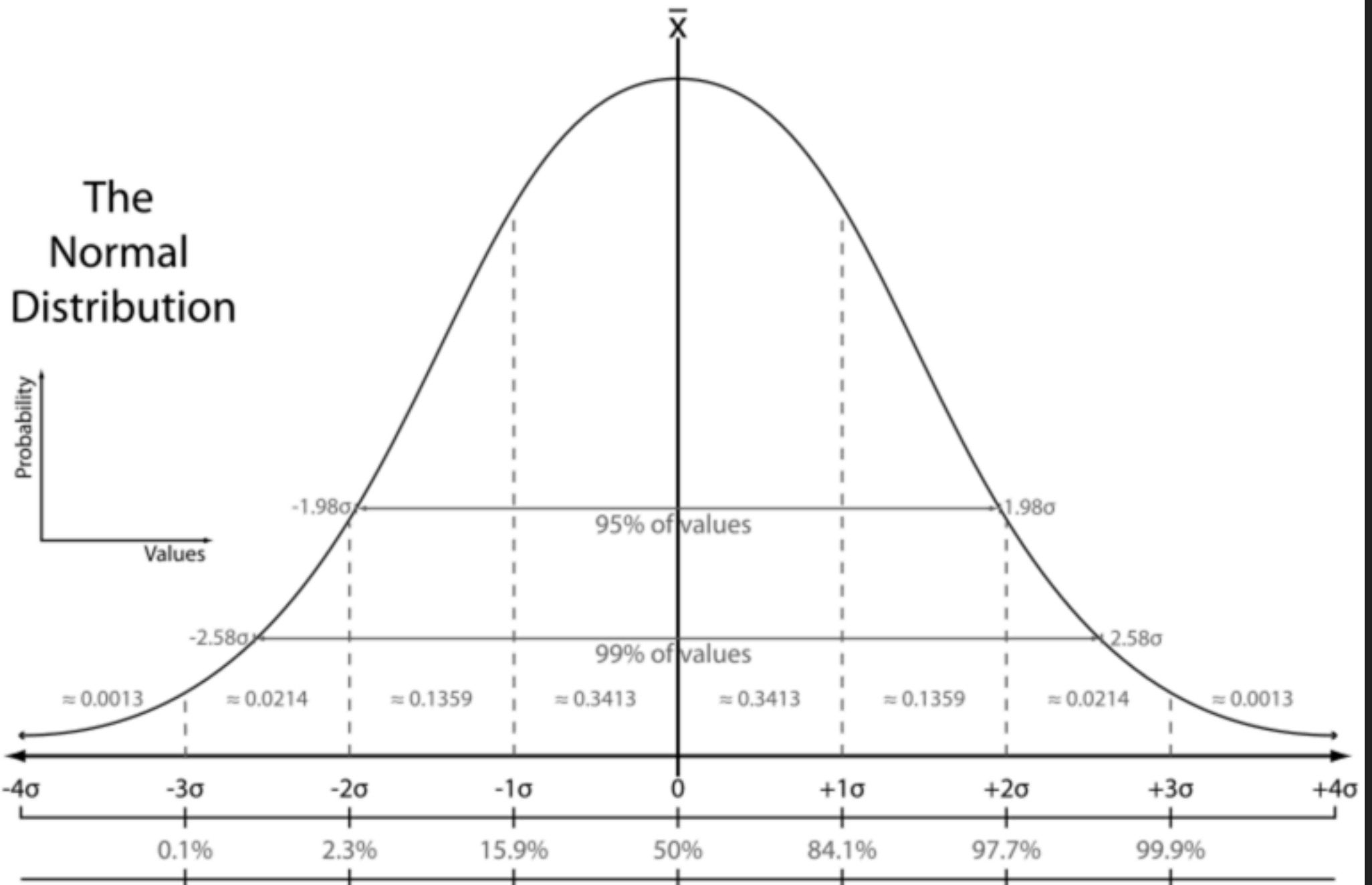


NORMAL DISTRIBUTION

$$P_x = \frac{m^x e^{-m}}{x!}$$

$$dP_x = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x-m)^2}{2\sigma^2}\right)$$

- For large m Poisson distribution \rightarrow normal distribution
- $\sigma = \sqrt{m}$
- For a lot of the events that we measure m is so large, we use the normal distribution even though a Poisson distribution would be more appropriate



VARIANCE AND STANDARD DEVIATION

- Definitions are valid for any distribution

- Variance:

$$\sigma^2 = \frac{1}{n} \sum_{i=0}^n (x_i - m)^2$$

- Standard deviation σ
- For normal distribution, $\sigma = \sigma$
- Practical variance (because m is not independent)

$$\sigma^2 = \frac{1}{n-1} \sum_{i=0}^n (x_i - x_{av})^2$$

EXAMPLE

- On average, we have $m=100$ photons on the CMOS sensor per s
- Poisson distribution
- 1s exposure: $\sigma = \sqrt{100} = 10$ $\sigma/m = 0.1$
- 100s exposure: $\sigma = \sqrt{10000} = 100$ $\sigma/m = 0.01$

EXAMPLE

- In reality, we are not photon limited
- Other noise sources dominate, including:
 - Thermal noise
 - CMOS Amplifier
 - Atmosphere
- Will assume normal distribution (note: there is a better way)
- Can use multiple measurement to estimate mean and variance
- We will do this for the photometry practical

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